

08

Tree Indexes –Part II



Intro to Database Systems
15-445/15-645
Fall 2019

AP

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Carnegie Mellon University

UPCOMING DATABASE EVENTS

Vertica Talk

- Monday Sep 23rd @ 4:30pm
- GHC 8102



TODAY'S AGENDA

More B+Trees

Additional Index Magic

Tries / Radix Trees

Inverted Indexes



B+TREE: DUPLICATE KEYS

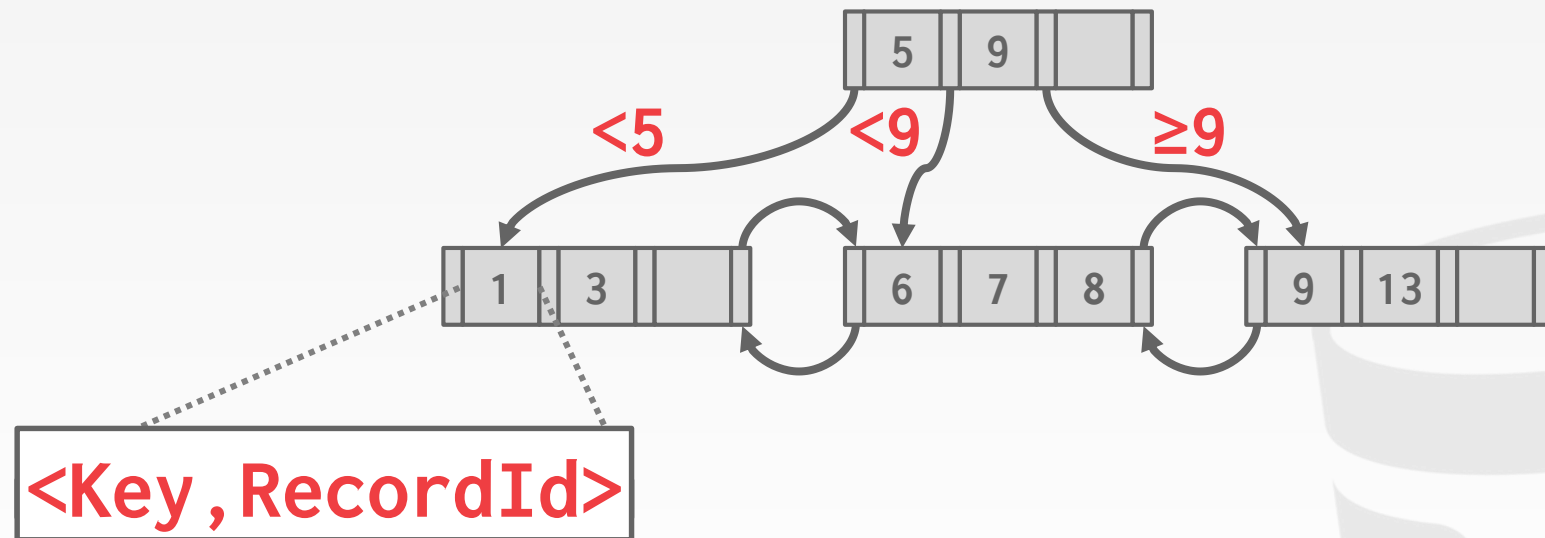
Approach #1: Append Record Id

- Add the tuple's unique record id as part of the key to ensure that all keys are unique.
- The DBMS can still use partial keys to find tuples.

Approach #2: Overflow Leaf Nodes

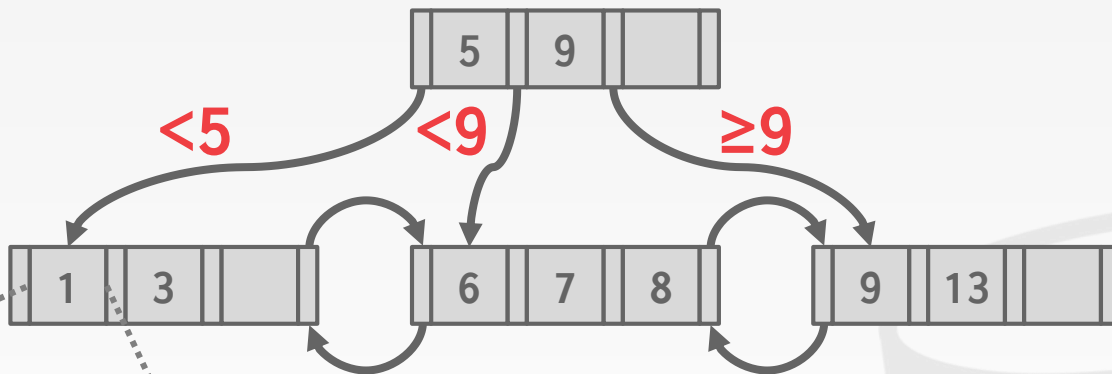
- Allow leaf nodes to spill into overflow nodes that contain the duplicate keys.
- This is more complex to maintain and modify.

B+TREE: APPEND RECORD ID



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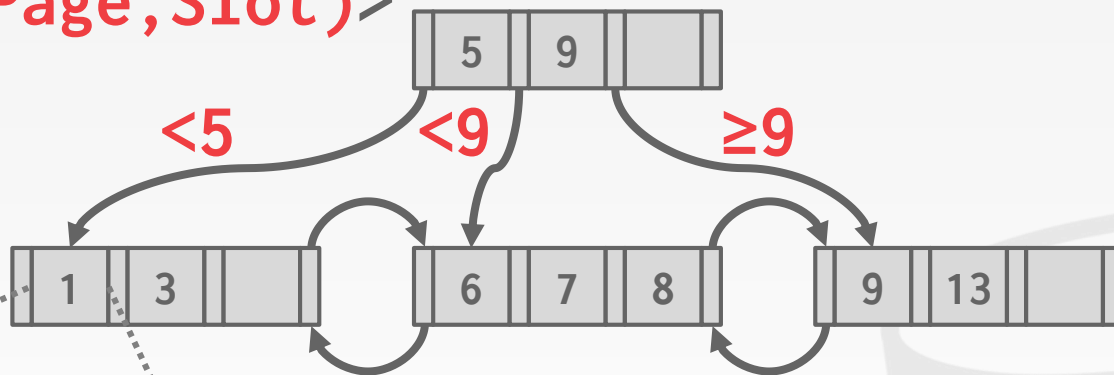
Insert 6



$\langle \text{Key}, \text{RecordId} \rangle$

B+TREE: APPEND RECORD ID

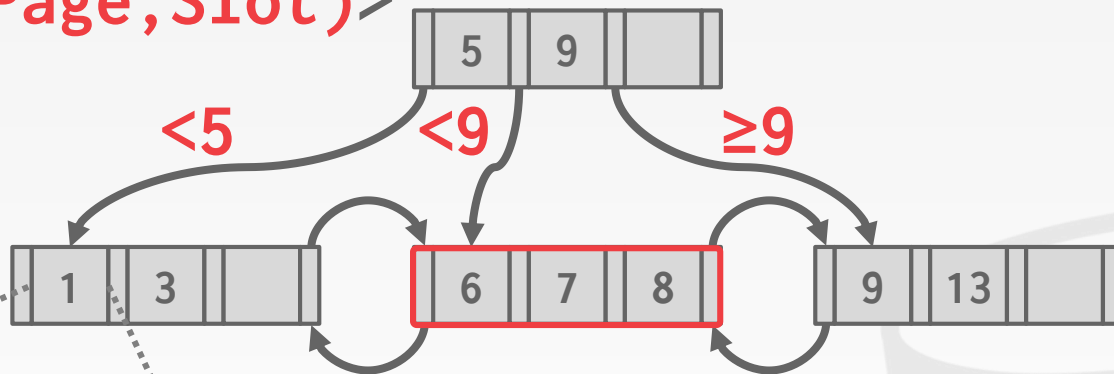
Insert $\langle 6, (\text{Page}, \text{Slot}) \rangle$



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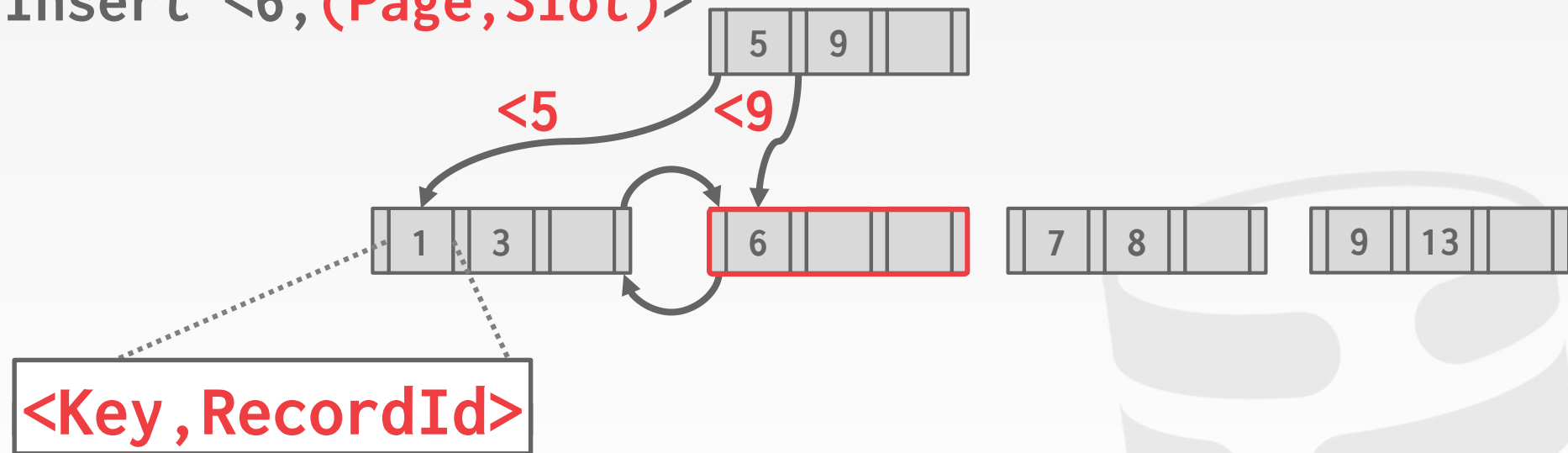
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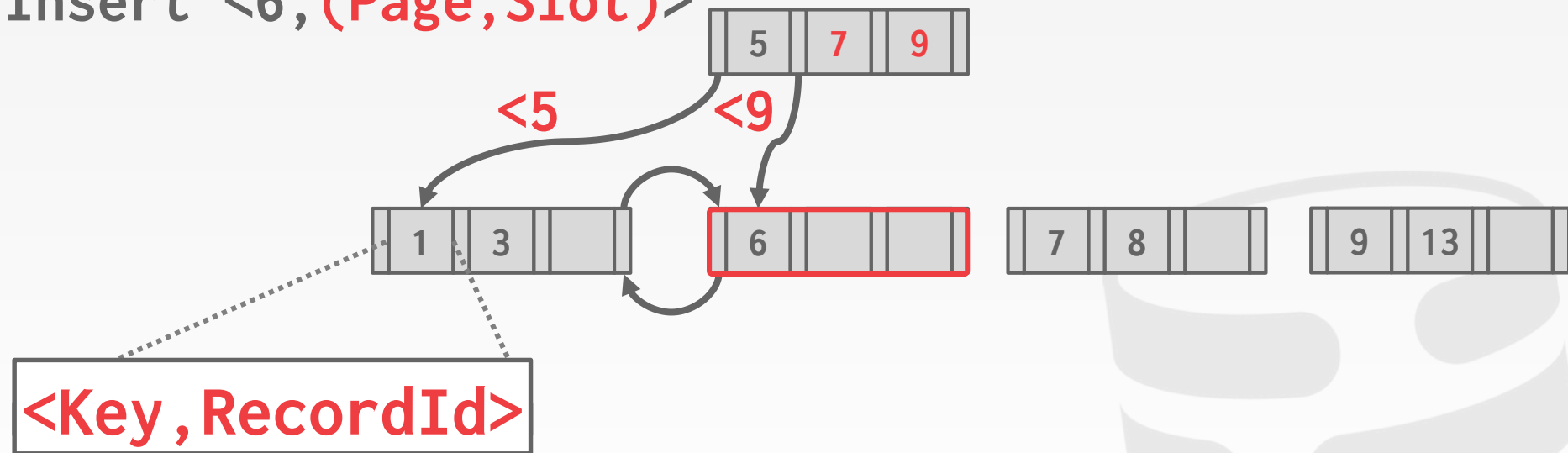
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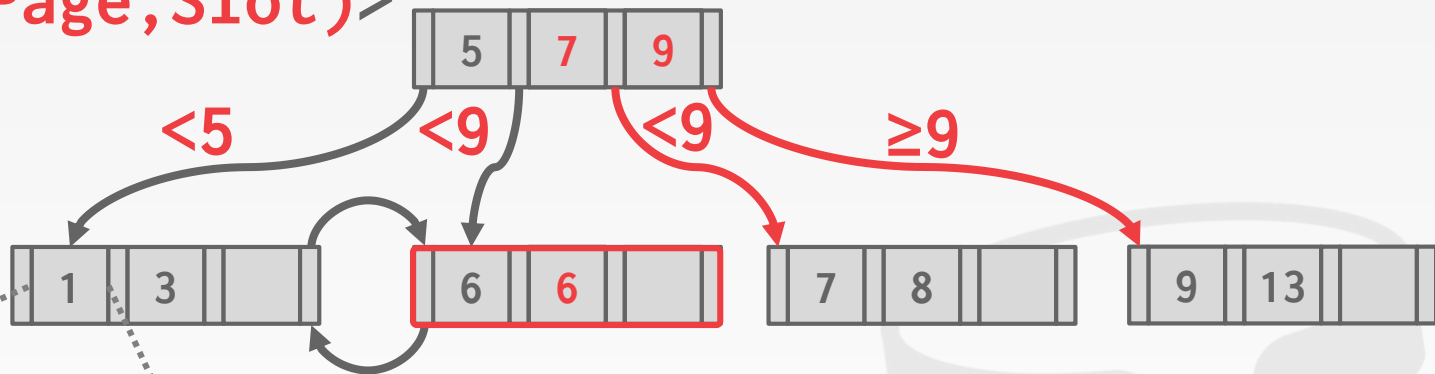
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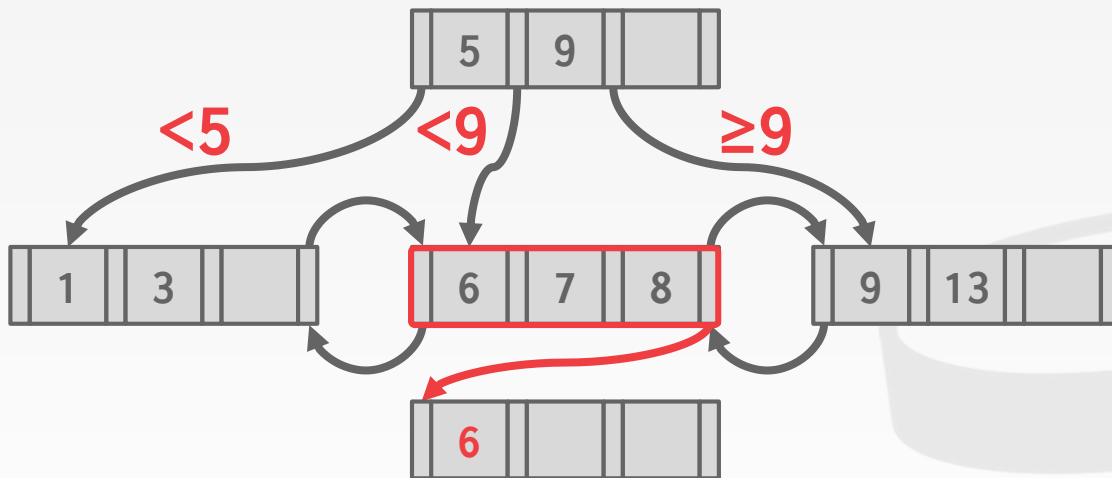
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B+TREE: OVERFLOW LEAF NODES

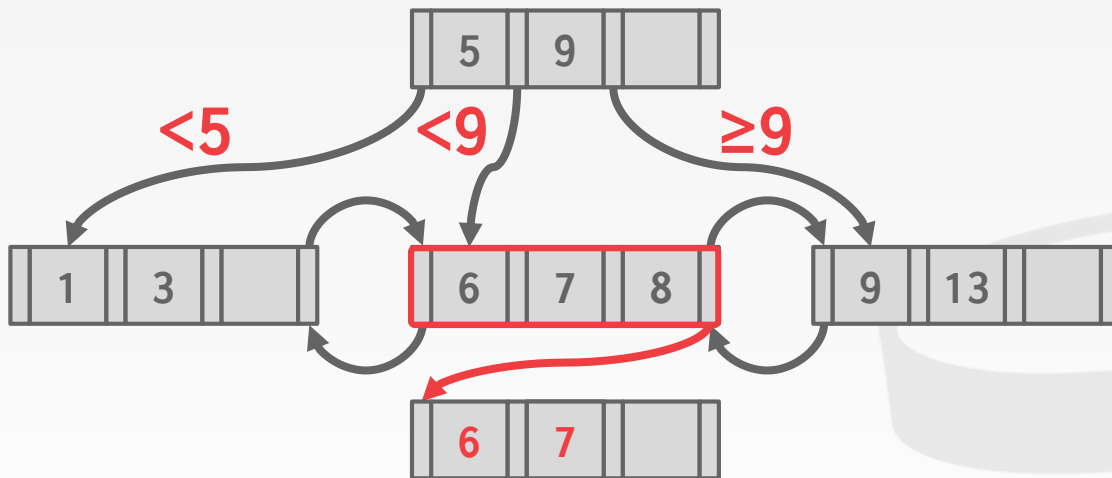
Insert 6



B+TREE: OVERFLOW LEAF NODES

Insert 6

Insert 7

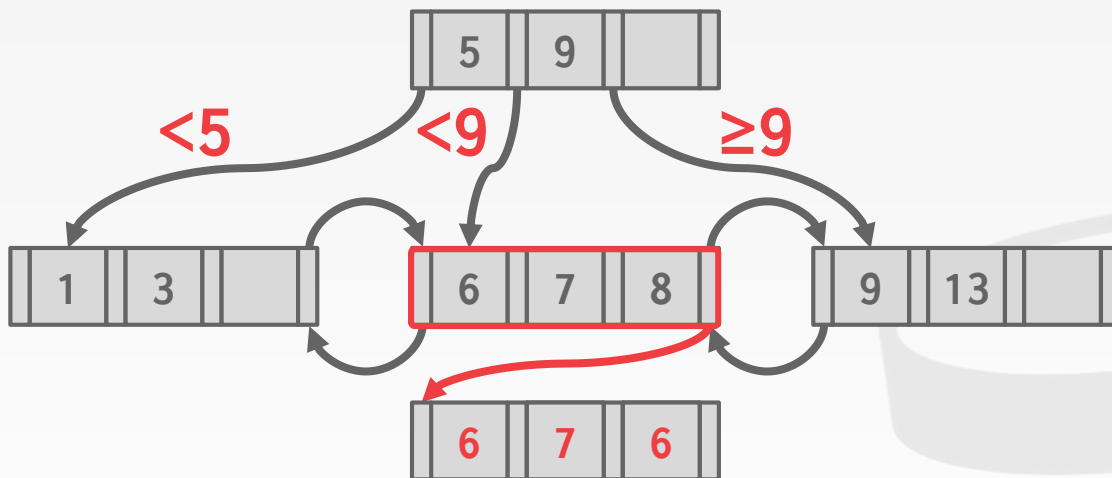


B+TREE: OVERFLOW LEAF NODES

Insert 6

Insert 7

Insert 6



DEMO

B+Tree vs. Hash Indexes
Table Clustering



IMPLICIT INDEXES

Most DBMSs automatically create an index to enforce integrity constraints but not referential constraints (foreign keys).

- Primary Keys
- Unique Constraints

```
CREATE TABLE foo (  
  id SERIAL PRIMARY KEY,  
  val1 INT NOT NULL,  
  val2 VARCHAR(32) UNIQUE  
);
```

```
CREATE UNIQUE INDEX foo_pkey  
  ON foo (id);
```

```
CREATE UNIQUE INDEX foo_val2_key  
  ON foo (val2);
```



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PARTIAL INDEXES

Create an index on a subset of the entire table. This potentially reduces its size and the amount of overhead to maintain it.

One common use case is to partition indexes by date ranges.

→ Create a separate index per month, year.

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CREATE INDEX idx_foo  
      ON foo (a, b)  
      WHERE c = 'WuTang';
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SELECT b FROM foo  
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COVERING INDEXES

If all the fields needed to process the query are available in an index, then the DBMS does not need to retrieve the tuple.

This reduces contention on the DBMS's buffer pool resources.

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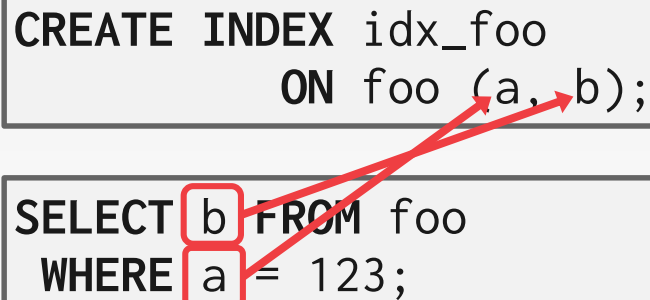
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Embed additional columns in indexes to support index-only queries.

These extra columns are only stored in the leaf nodes and are not part of the search key.

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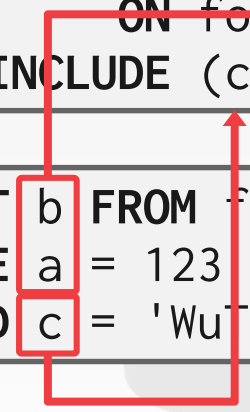
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FUNCTIONAL/EXPRESSION INDEXES

An index does not need to store keys in the same way that they appear in their base table.

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SELECT * FROM users
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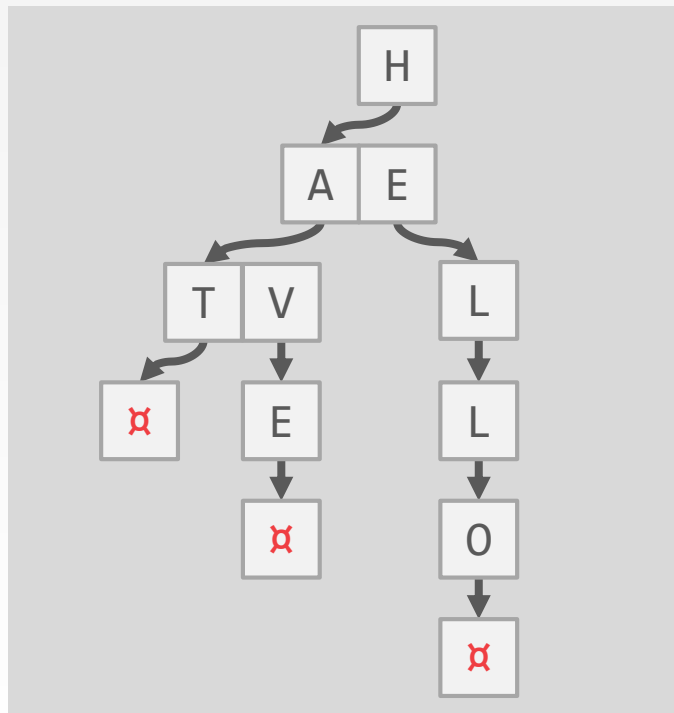
OBSERVATION

The inner node keys in a B+Tree cannot tell you whether a key exists in the index. You must always traverse to the leaf node.

This means that you could have (at least) one buffer pool page miss per level in the tree just to find out a key does not exist.

TRIE INDEX

Keys: HELLO, HAT, HAVE

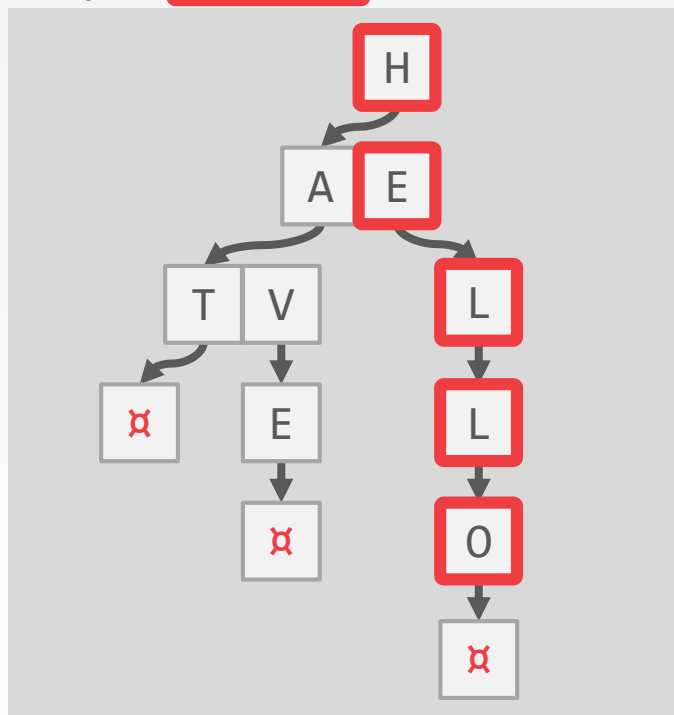


Use a digital representation of keys to examine prefixes one-by-one instead of comparing entire key.

→ Also known as *Digital Search Tree*, *Prefix Tree*.

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TRIE INDEX PROPERTIES

Shape only depends on key space and lengths.

- Does not depend on existing keys or insertion order.
- Does not require rebalancing operations.

All operations have $O(k)$ complexity where k is the length of the key.

- The path to a leaf node represents the key of the leaf
- Keys are stored implicitly and can be reconstructed from paths.

TRIE KEY SPAN

The **span** of a trie level is the number of bits that each partial key / digit represents.

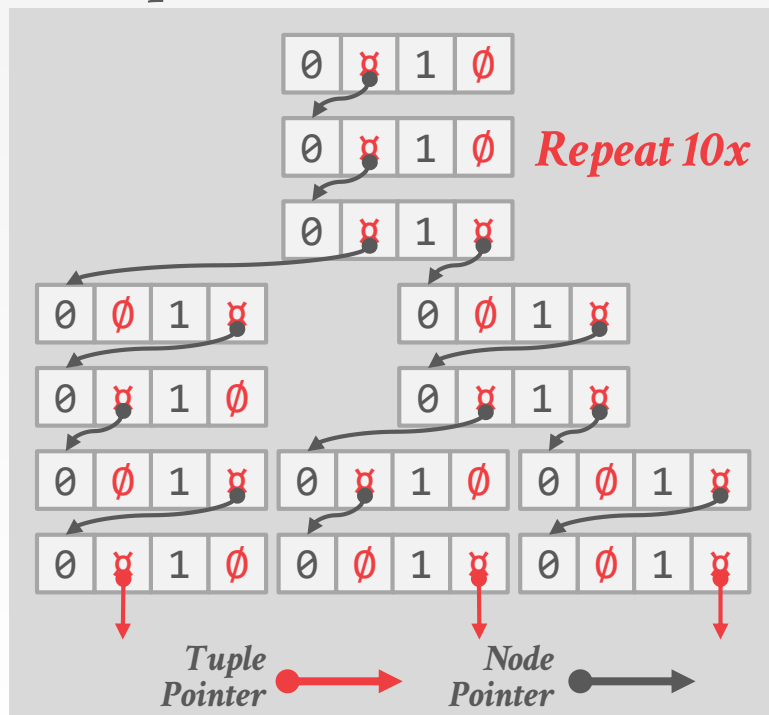
→ If the digit exists in the corpus, then store a pointer to the next level in the trie branch. Otherwise, store null.

This determines the **fan-out** of each node and the physical **height** of the tree.

→ *n*-way Trie = Fan-Out of *n*

TRIE KEY SPAN

1-bit Span Trie



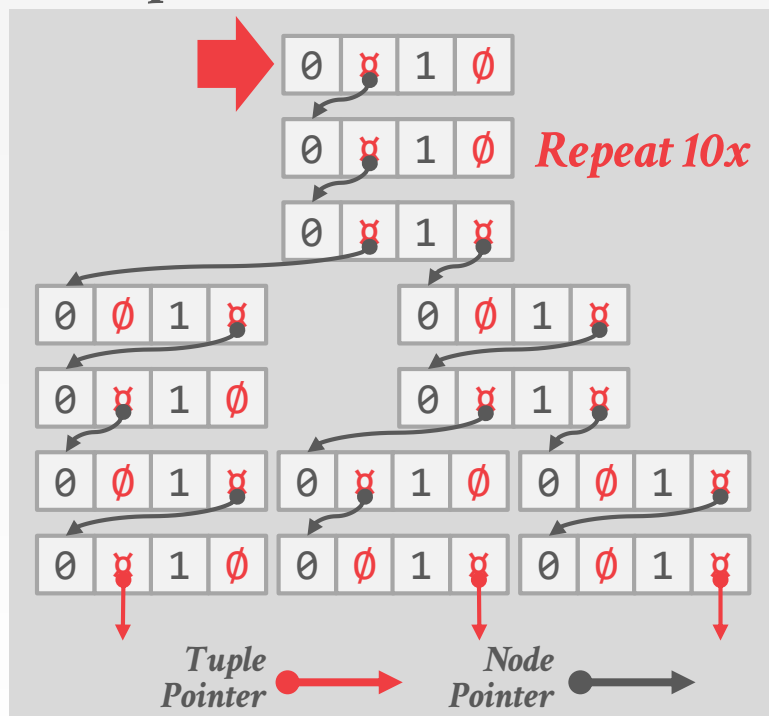
K10→ 00000000 00001010

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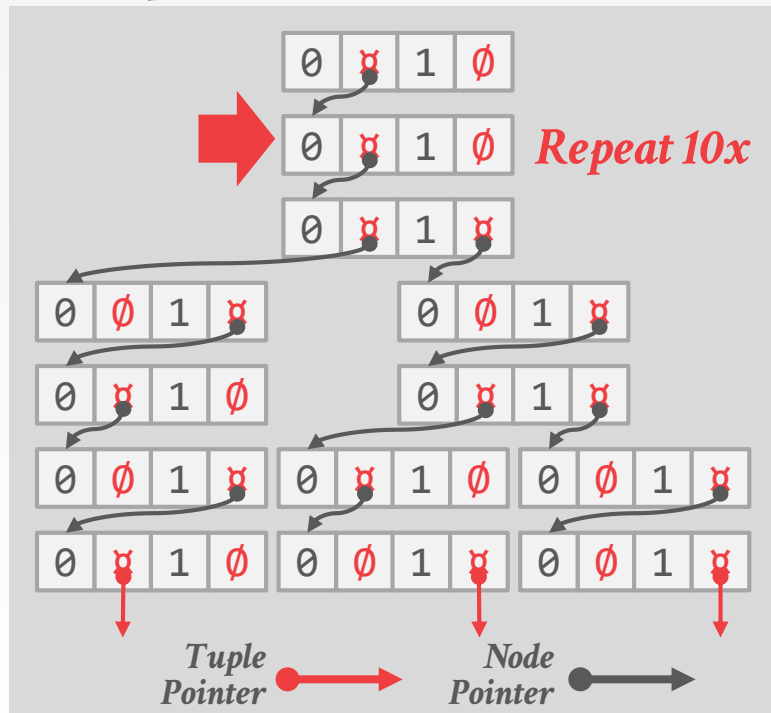
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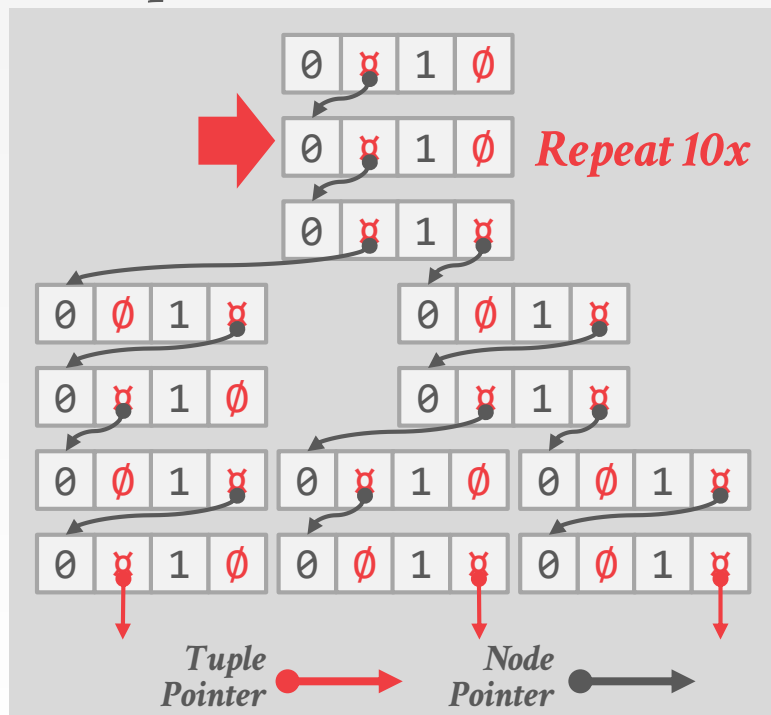
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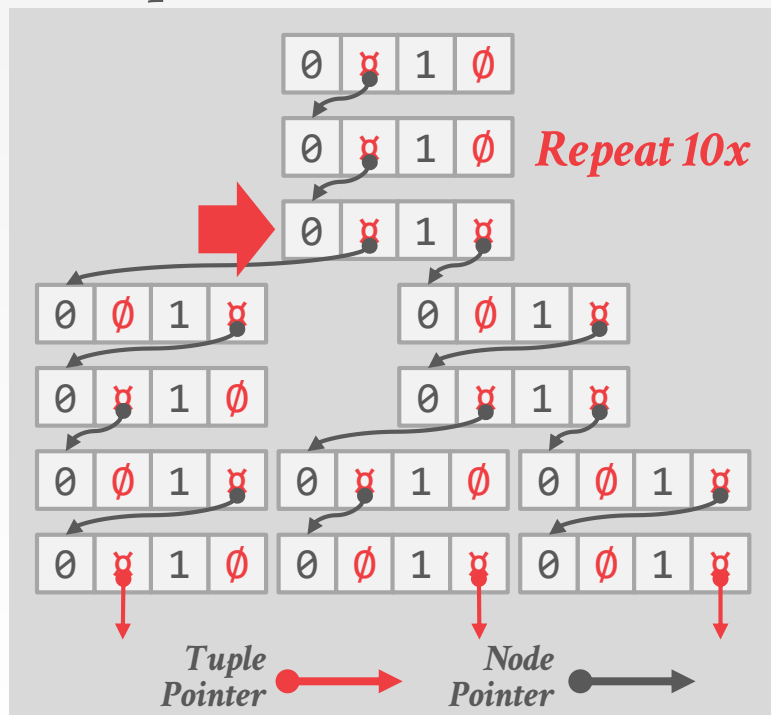
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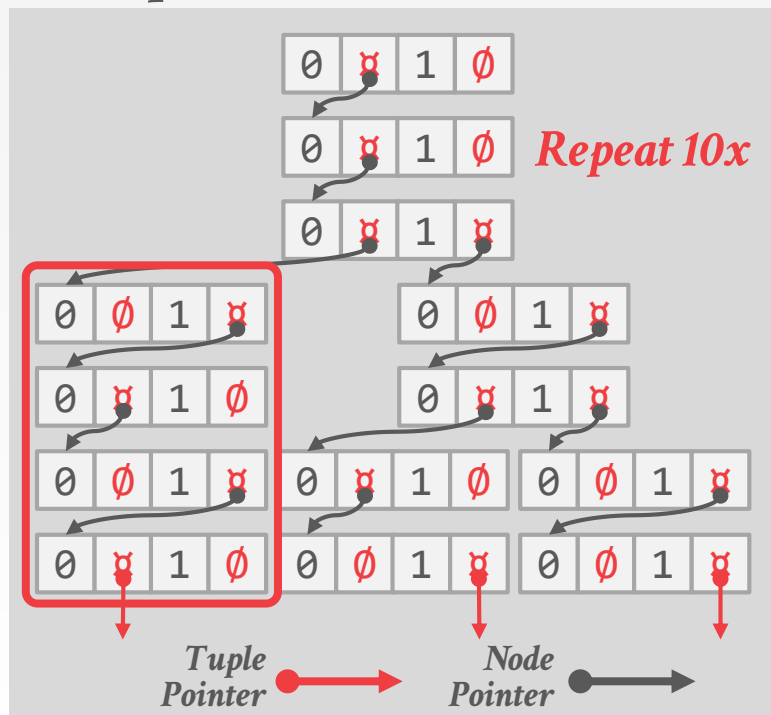
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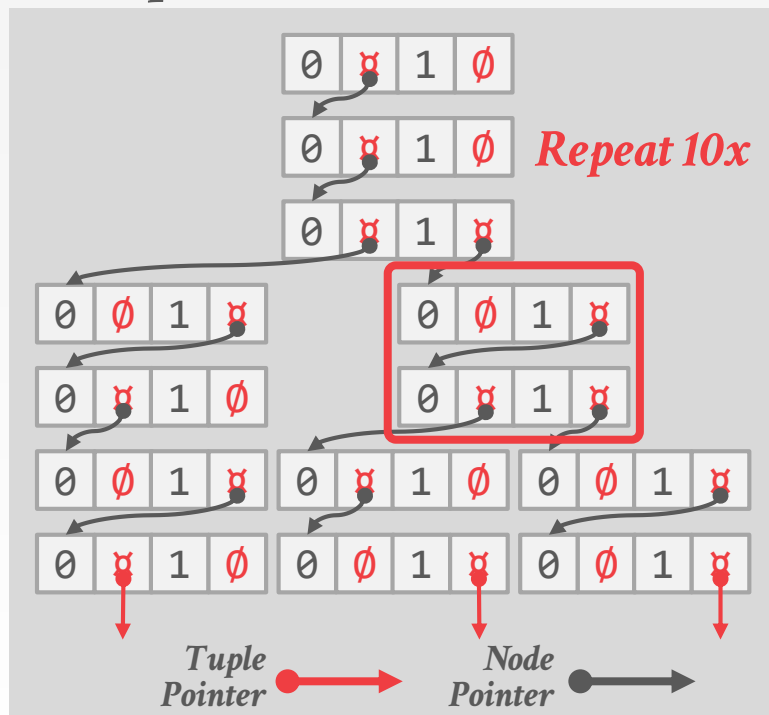
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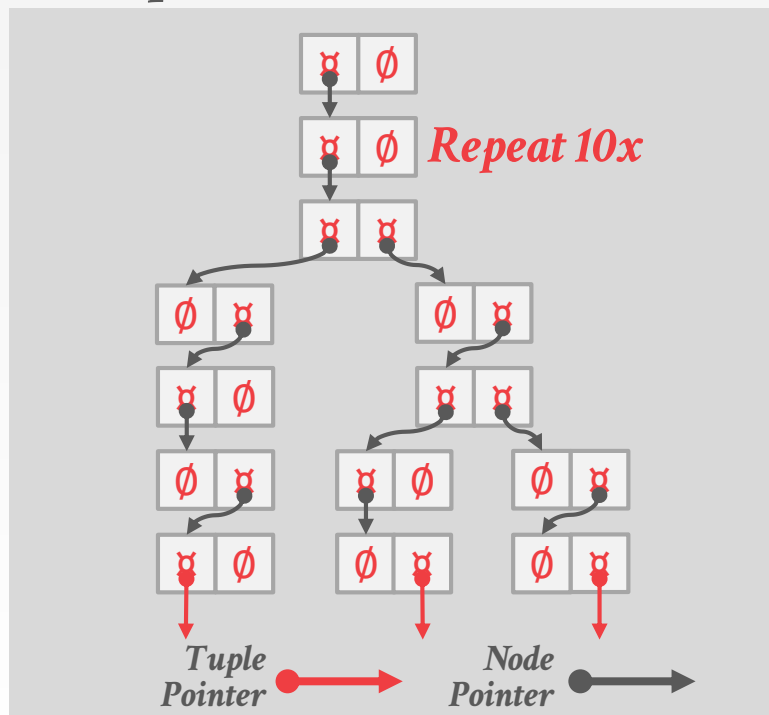
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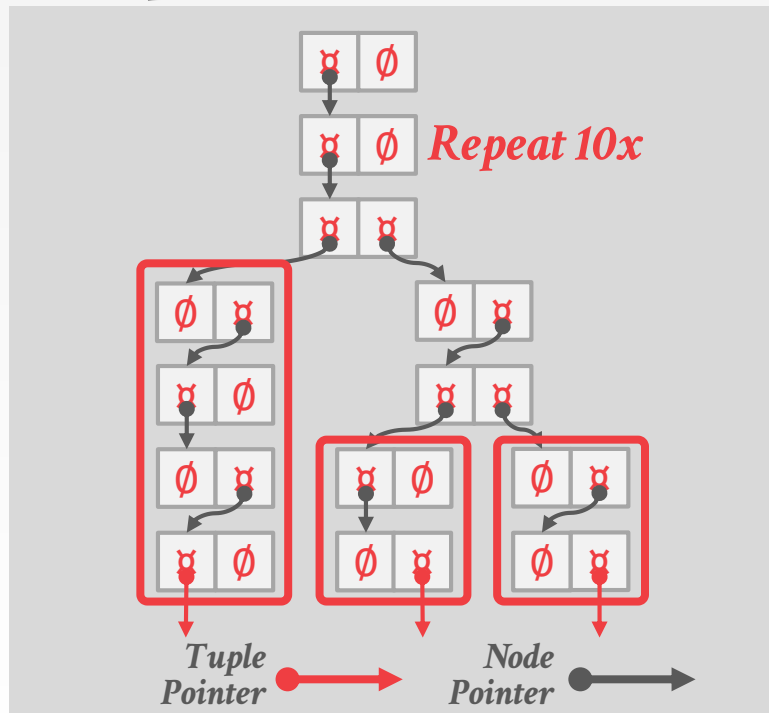
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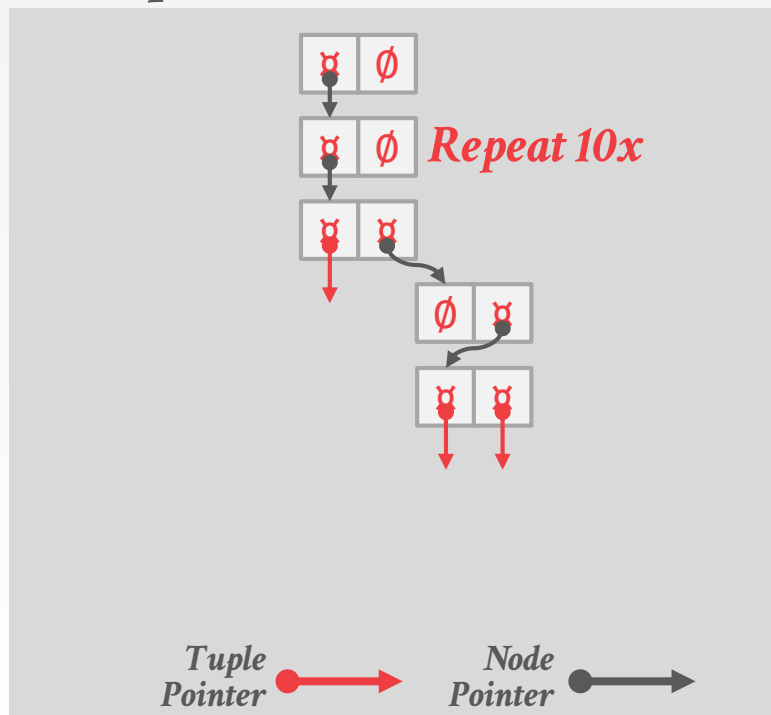
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RADIX TREE

1-bit Span Radix Tree

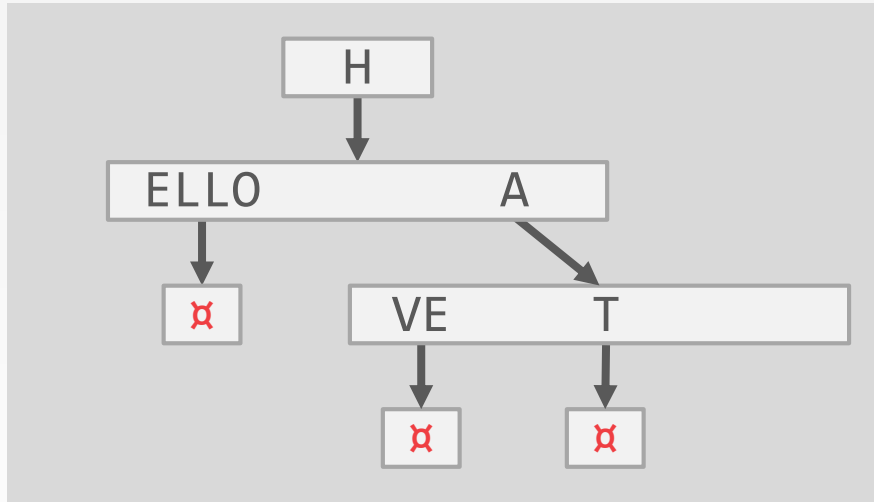


Omit all nodes with only a single child.

→ Also known as *Patricia Tree*.

Can produce false positives, so the DBMS always checks the original tuple to see whether a key matches.

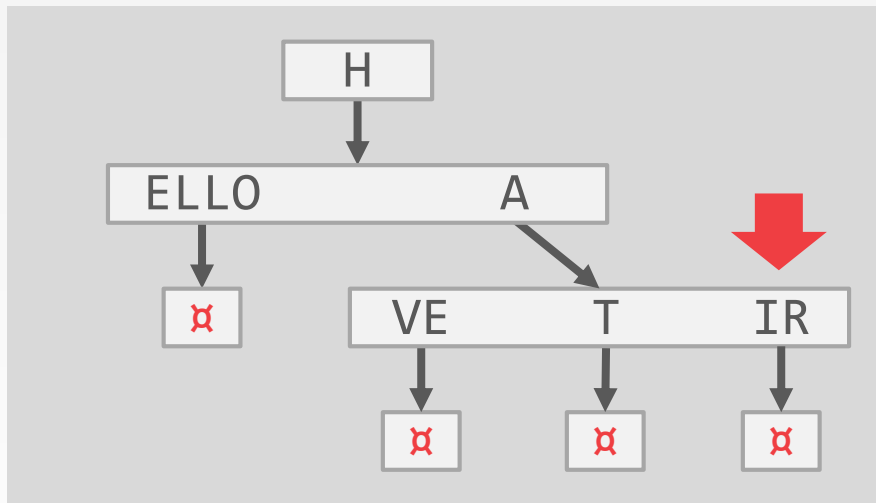
RADIX TREE: MODIFICATIONS



Insert HAIR

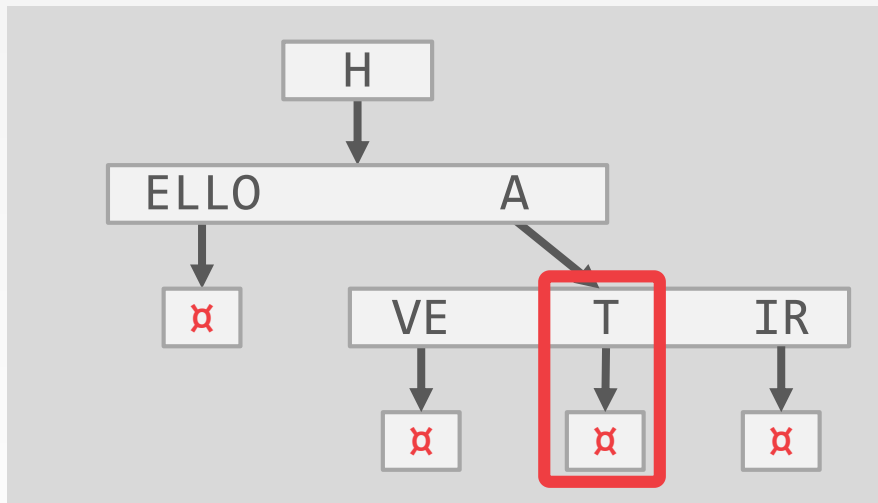


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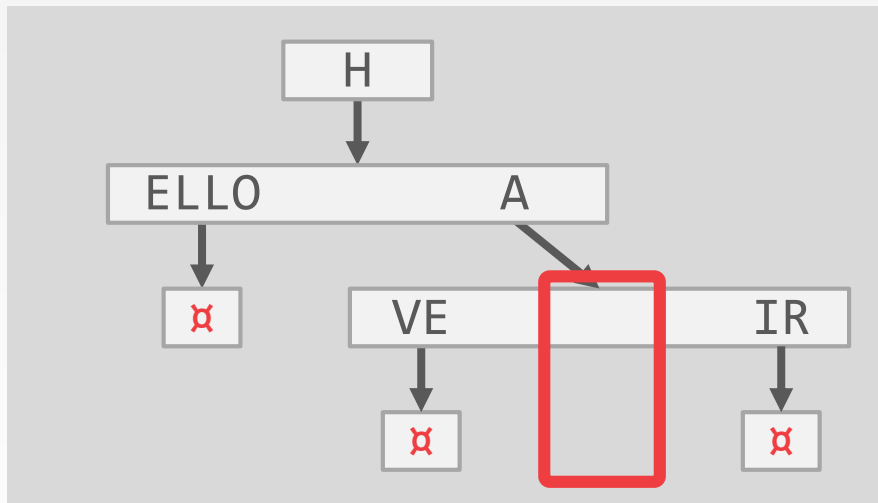
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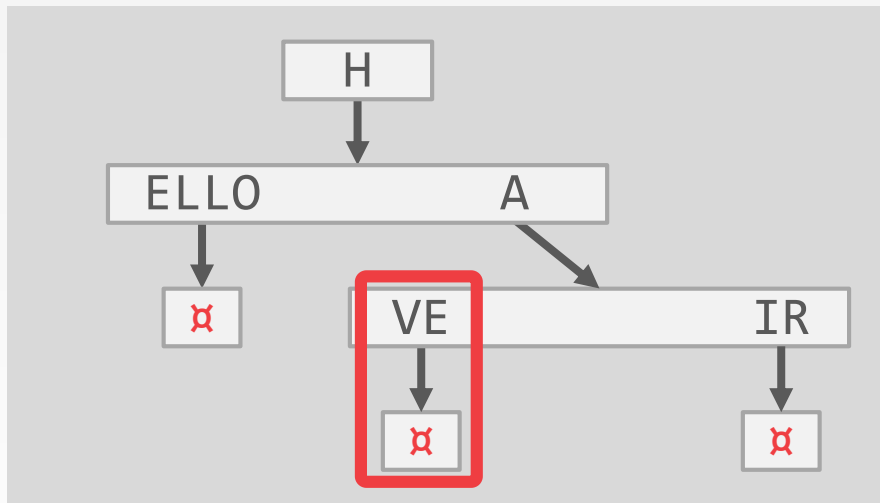
Insert HAIR
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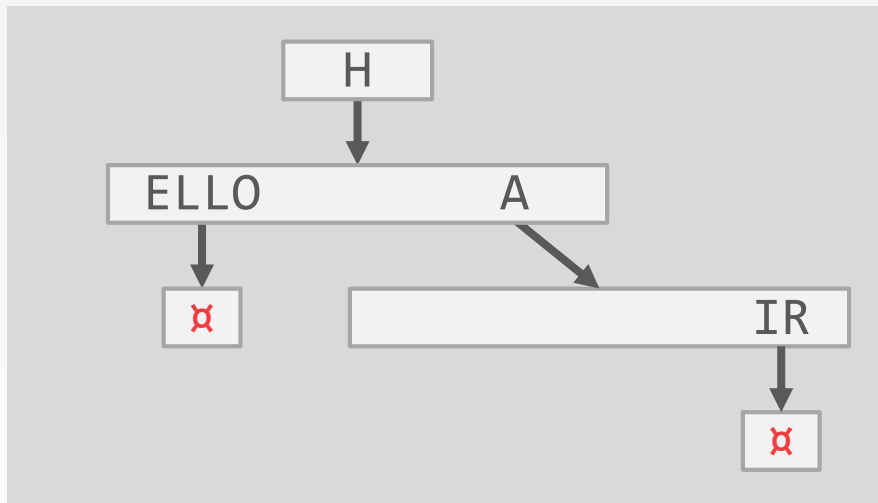
Insert HAIR
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RADIX TREE: MODIFICATIONS



Insert HAIR
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RADIX TREE: MODIFICATIONS

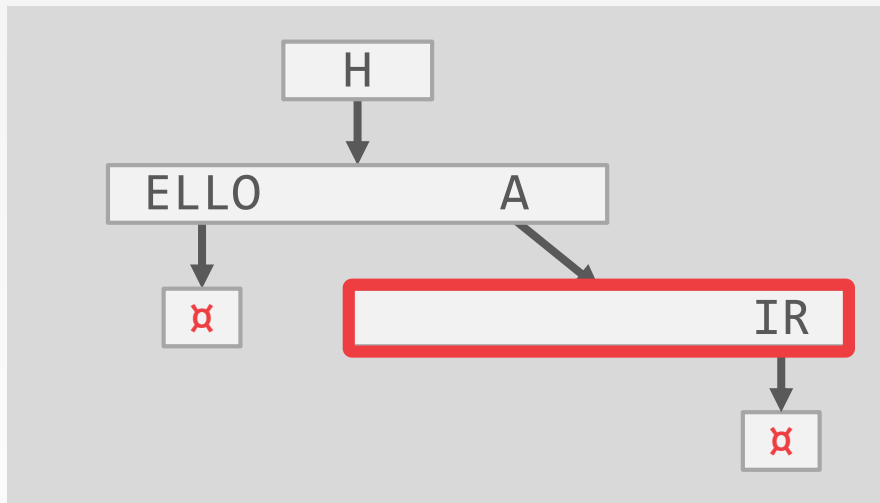


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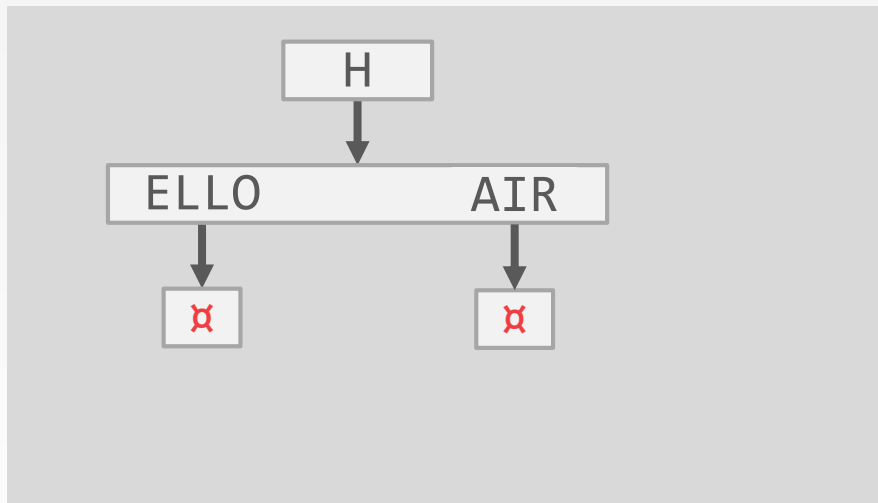
Delete HAVE

RADIX TREE: MODIFICATIONS



Insert HAIR
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RADIX TREE: MODIFICATIONS



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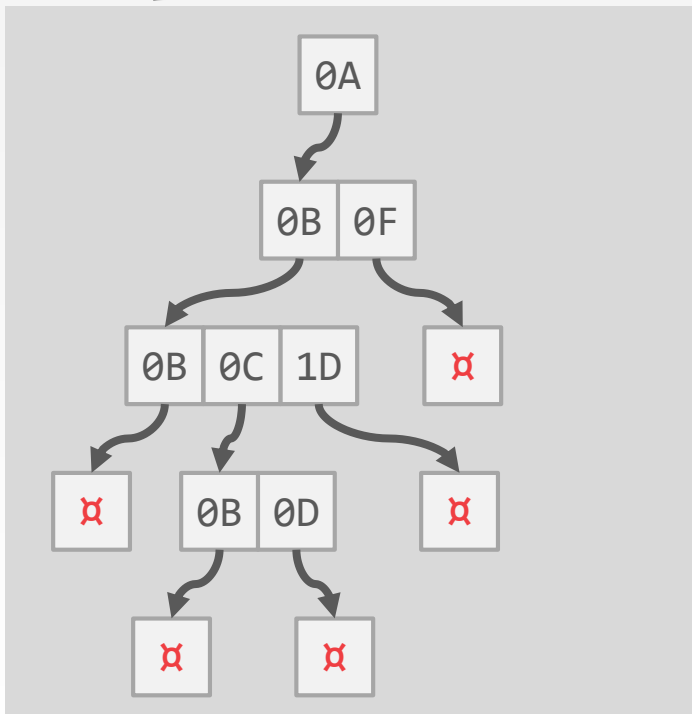
RADIX TREE: BINARY COMPARABLE KEYS

Not all attribute types can be decomposed into binary comparable digits for a radix tree.

- **Unsigned Integers:** Byte order must be flipped for little endian machines.
- **Signed Integers:** Flip two's-complement so that negative numbers are smaller than positive.
- **Floats:** Classify into group (neg vs. pos, normalized vs. denormalized), then store as unsigned integer.
- **Compound:** Transform each attribute separately.

RADIX TREE: BINARY COMPARABLE KEYS

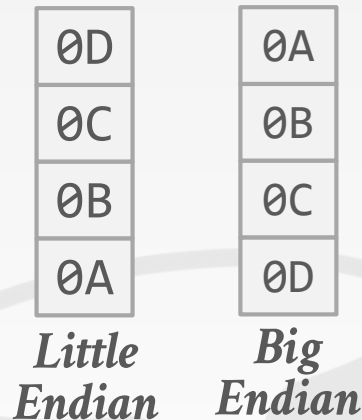
8-bit Span Radix Tree



Int Key: 168496141

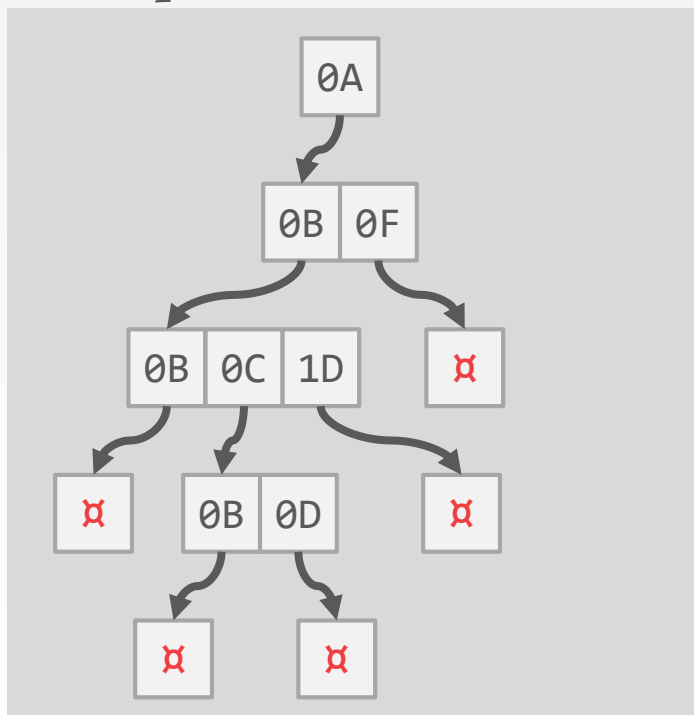


Hex Key: 0A 0B 0C 0D



RADIX TREE: BINARY COMPARABLE KEYS

8-bit Span Radix Tree



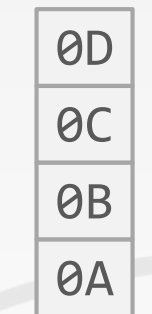
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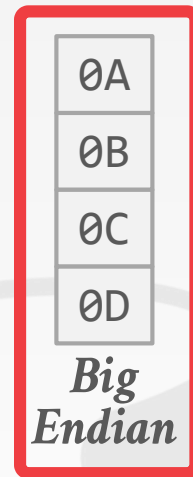
Hex Key: 0A 0B 0C 0D

Find 658205

Hex 0A 0B 1D



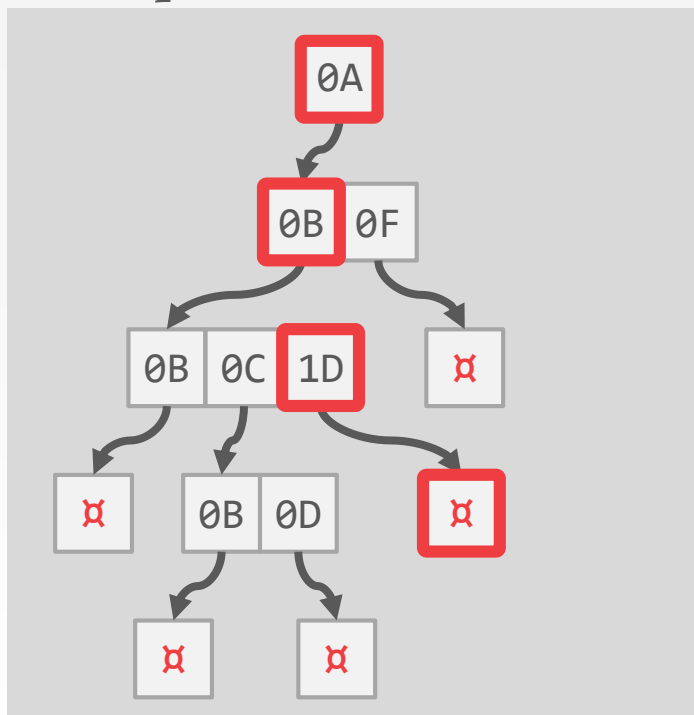
*Little
Endian*



*Big
Endian*

RADIX TREE: BINARY COMPARABLE KEYS

8-bit Span Radix Tree



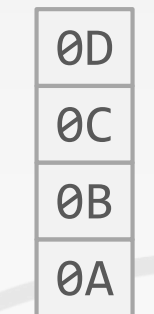
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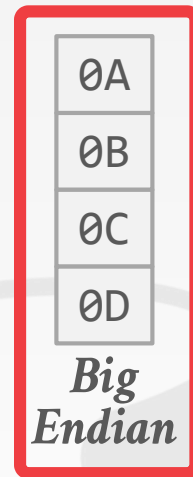
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*Little
Endian*



*Big
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OBSERVATION

The tree indexes that we've discussed so far are useful for "point" and "range" queries:

- Find all customers in the 15217 zip code.
- Find all orders between June 2018 and September 2018.

They are **not** good at keyword searches:

- Find all Wikipedia articles that contain the word "Pavlo"

WIKIPEDIA EXAMPLE

```
CREATE TABLE useracct (  
  userID INT PRIMARY KEY,  
  userName VARCHAR UNIQUE,  
  :  
);
```

```
CREATE TABLE pages (  
  pageID INT PRIMARY KEY,  
  title VARCHAR UNIQUE,  
  latest INT  
  REFERENCES revisions (revID),  
);
```

```
CREATE TABLE revisions (  
  revID INT PRIMARY KEY,  
  userID INT REFERENCES useracct (userID),  
  pageID INT REFERENCES pages (pageID),  
  content TEXT,  
  updated DATETIME  
);
```

WIKIPEDIA EXAMPLE

If we create an index on the content attribute, what does that do?

```
CREATE INDEX idx_rev_cntnt  
  ON revisions (content);
```

This doesn't help our query.
Our SQL is also not correct...

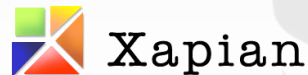
```
SELECT pageID FROM revisions  
  WHERE content LIKE '%Pavlo%';
```

INVERTED INDEX

An *inverted index* stores a mapping of words to records that contain those words in the target attribute.

- Sometimes called a *full-text search index*.
- Also called a *concordance* in old (like really old) times.

The major DBMSs support these natively.
There are also specialized DBMSs.



QUERY TYPES

Phrase Searches

→ Find records that contain a list of words in the given order.

Proximity Searches

→ Find records where two words occur within *n* words of each other.

Wildcard Searches

→ Find records that contain words that match some pattern (e.g., regular expression).

DESIGN DECISIONS

Decision #1: What To Store

- The index needs to store at least the words contained in each record (separated by punctuation characters).
- Can also store frequency, position, and other meta-data.

Decision #2: When To Update

- Maintain auxiliary data structures to "stage" updates and then update the index in batches.

CONCLUSION

B+Trees are still the way to go for tree indexes.

Inverted indexes are covered in [CMU 11-442](#).

We did not discuss geo-spatial tree indexes:

→ Examples: R-Tree, Quad-Tree, KD-Tree

→ This is covered in [CMU 15-826](#).

NEXT CLASS

How to make indexes thread-safe!

